Maintenance of Binary Topological Constraints through Active Databases

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Abstract

This paper presents a system developed at UNICAMP for automatically maintaining topological constraints in a geographic database. This system is based on extending to spatial data the notion of standard integrity maintenance through active databases. Topological relations, defined by the user, are transformed into spatial integrity constraints, which are stored in the database as production rules. These rules are used to maintain the corresponding set of topological relations, for all applications that use the database. This extends previous work on rules and GIS by incorporating the rules into the DBMS rather than having them handled by a separate module.

Keywords: Active databases, topological relations, spatial integrity

1 Introduction

Active databases are systems that respond to events generated internally or externally to the system itself without user intervention. The active dimension is supported by production rule mechanisms, provided by the database management system (DBMS). Production rules are usually defined as clauses if X then Y, where X is a predicate to be tested, and Y is an action to be performed if the predicate is satisfied. Active databases have been suggested as an appropriate solution for constraint maintenance in the case of standard applications. No experiment has been made, however, of applying these ideas to georeferenced data.

The use of rules in GIS is usually treated either by means of an external mechanism which is coupled to the geographic database or in the context of deductive systems. The integration and management of spatial relations within an active DBMS provides the following advantages over the standard rule-based approaches:

• the specification and preservation of spatial relations is handled by the DBMS itself, regardless of any application code, allowing independent evolution of both data and application;
• the same underlying geographic database may be used by all applications that need to have the same view of the world, without requiring application rewriting for constraint checking;
• different applications can have distinct views of the same database, by enabling and disabling different sets of rules;
• spatial relations can be treated at the same architectural level as the data they refer to. This helps low level implementation issues, such as leaving the optimization of spatial operations to the DBMS.

The results presented in this paper are part of an ongoing research at UNICAMP, to extend the paradigm of active database systems to incorporate maintenance of spatial relations in the presence of updates. Given, however, the theoretical and implementation problems in specifying and maintaining general spatial constraints among georeferenced entities, we have so far restricted ourselves to the important problem of binary topological constraints among objects stored in vector format. This solution has been implemented at the Department of Computer Science, UNICAMP.

The main results presented are the following:

• description of an extended active database architecture for managing georeferenced data;
• overview of the active DBMS prototype developed to enforce topological binary relations.

The theoretical background adopted here for specifying binary relations is based on [Cev03]; the active database system was implemented by combining the results reported in [CAM93] with the object oriented spatial data model of [CFS94]. The prototype described in the paper is being tested on vector data collected for different kinds of phenomena in a specific region of the state of São Paulo, in the domain of telecommunications planning. Data samples are being provided by the R&D Telecommunication Center at Campinas, who are also responsible for the definition of the topological relations. The tests performed correspond therefore to current real world conditions.

This paper is organized as follows. Section 2 describes present research in the area of GIS and rule-based systems. Section 3 gives an overview of the theoretical basis for defining binary topological relations, and their inclusion in an object georeferenced data model. Section 4 describes the prototype developed. Section 5 shows how topological constraints were implemented as rules in this prototype. Finally, section 6 presents conclusions and future directions.
Active object-oriented DBMSs have proved useful in the area of scientific database applications. The most common application for active databases is integrity maintenance. An integrity constraint, in a database environment, is a statement of a condition that must be met in order to maintain data consistency. DBMSs have limited support for automatic maintenance of integrity constraints. Active databases are a solution to this problem, since rules can be activated upon update requests. Constraint specification and maintenance can then be kept independent from application development. The paradigm of active databases is useful for implementing or extending several database functions. Examples of present research in active databases are described in [Cha92, Buc94].

The basic model for active DBMSs is by [DBM88], where a production rule is specified as a triple (E, C, A). This can be translated into the statement When E If C Then A. E stands for the Event upon which the rule is triggered, C the Condition to be tested, and A the Action to be performed if the condition is met. Events may be internal to the database (e.g., queries, updates), or external (e.g., hardware interrupts). Conditions are usually predicates over the database (e.g., queries, updates), or external (e.g., hardware interrupts). Actions are expressed in the database programming language and may range from atomic actions to complete programs. From now on, the term rule in this paper will denote this triple.

In an active DBMS, rules are stored and managed together with data. The activation and computation of rules are basically performed in three steps [MT94]:

- **rule triggering**: a given Event is signalled, which demands checking the rule(s) to be executed (fired). This step requires going through the stored rules to select the appropriate ones.
- **rule evaluation**: the Condition part of the chosen rule is checked, to verify if it is satisfied;
- **rule execution**: the Action part of the rule is performed, if the condition is met.

The approach of combining rules and data handling is not new in the area of GIS research. In such a context, rules are used in a deductive role: they help process queries, perform data analysis or derive relationships among data. However, in most cases, rules are not integrated at the data management level (as opposed to the active database philosophy). Rather, rules and data are treated by different handlers as isolated components (the rule management system and the database management system), which need intermediate modules to allow their communication. Usually, GIS that contemplate rules rely on coupling modules for handling georeferenced data (e.g., for analysis or display) to an external rule management system. The integration of these components is provided by an expert system shell, which also supports spatial decision making (see, for instance, [AD90]).

Coupling the rule base to the database then requires several levels of modelling and translation among modules, as well as demands that the user learn different languages (to access data and to specify rules). A typical example of such an approach appears in [KWB93]. In this research, Arc Info provides the spatial data and a rule base is used to feed a reasoning program for classification, refinement and generalization.

Other examples of research in rules and georeferenced data are the use of expert system shells ([SR93, SRD+91, LL93]), spatial decision support systems built by coupling spatial databases and rule sets ([NS91, AYA+92]), expert systems for dense map name placement ([DF92], rule based systems for querying [Wcy98] or deductive systems based on PROLOG [Web99]. Such approaches are not satisfactory from a data management point of view. They may make applications very sensitive to modifications in the relations among data, and leave to programmers the burden of having to know and check all relevant constraints at each step. These solutions are language-based and therefore require additional effort to integrate the rule programming language with the chosen DBMS.

The mismatch between the chosen rule language and the GIS database demand that users create complete new programs for each data analysis performed using the rules. Typically, users are required to apply successive sets of queries, store the results in intermediate files, and then apply the chosen set of analysis and correlation rules among these files (e.g., [LHM94]). The active database approach, on the other hand, allows the insertion of rules in the database which can then be used in combining results of queries without these intermediate steps.

Some steps towards bridging the gap between rules and database management can be found in, for instance, [SA93], [PMP93, AWP93]. [PMP93] discuss the importance of a rule management component as an integral part of a spatial database. One approach is to consider rules during the database modelling process: in [SA93], rules are modelled as a specific class in an object oriented design methodology for geographic systems and implemented in an object oriented language. Another approach is the use of deductive databases: [AWP93] analyze topological relationships expressed in a logic language within a deductive database, but the emphasis is on constraint specification and not maintenance.

### 3 Topological relations - adopted model

This section presents the model adopted for topological relations, and the algorithm for transforming them into (E, C, A) rules.

[Cut94] distinguishes between the following classes of spatial relationships:

- **topological relations** - those that are invariant under topological transformations like translation, scaling or rotation. Examples are adjacent, inside, disjoint.
- **direction relations** - those that establish relative positioning of elements within some positioning system (e.g., north, south).
- **metric relations** - those that can be expressed in scalar form defining measurement values (e.g., distance).

Our model for defining topological constraints is based on [Cev093]. This work originated with the definition of the 4-intersection model (see [EF91]), which describes binary topological relations among area objects (connected regions without holes), later extended by [HT92] to include line and point objects.

The 4-intersection model considers all the binary combinations of region intersection: a region $A$ is a 2D point set with a connected interior $A^I$ and boundary $B$. If the exterior $A^{-1}$ is considered, one obtains the 5-intersection...
matrix. As stressed in [CSE94], the 9-intersection matrix forms the base set from which database users can construct more complex relationships that are appropriate to their application domain. The 4-intersection and the 9-intersection matrices are shown below, depicting all types of intersection between two areas (regions) $A$ and $B$. For instance, element $(2,2)$ of the matrix indicates whether the boundaries of $A$ and $B$ intersect. The third column and the third row belong to the 9-intersection matrix and correspond to including the exterior of $A$ or $B$ in the intersection evaluation.

$\begin{array}{cccc} A^0 \cap B^0 & A^0 \cap B^- & A^0 \cap \overline{B}^- & A^- \cap B^- \\ A^- \cap B^0 & A^- \cap B^- & A^- \cap \overline{B}^- & A^- \cap B^- \end{array}$

The 4-intersection matrices just indicate whether the intersection between two objects is empty or not, but not the nature of the intersection. [Cev93] extended the 4-intersection matrix to consider the dimension $\dim$ of the intersection between any two objects (the dimension-extended method) and showed formally that such an approach could be synthesized, for ease of handling by humans, into 5 mutually exclusive topological relationships. These relationships – touch, in, cross, overlap, disjoint – express when the dimension $\dim$ of the intersections between two objects can be empty, a point (0D), a line (1D) or an area (2D). In order to express all 52 valid binary relationships among these objects, [Cev93] also introduced three boundary operators, which allow returning the boundary of an object (a boundary line of an area or the two end points of a line).

All binary topological relations can be therefore checked against these five mutually exclusive relationships, being defined by the above expressions and boundary operators. The relationships between two objects $A$ and $B$ (of types line, point and area) can be expressed as follows:

- $(A \text{ in } B) \iff (A \cap B \neq A) \land (\dim(A^0 \cap B^0) = 0)$
- $(A \text{ touch } B) \iff (A^0 \cap B^0 = \emptyset) \land (A \cap B \neq \emptyset)$
- $(A \text{ cross } B) \iff (\dim(A^0 \cap B^0) = (\max(\dim(A^0)), \dim(B^0) - 1) \land (A \cap B \neq A) \land (A \cap B \neq \emptyset)$
- $(A \text{ overlap } B) \iff (\dim(A^0) = \dim(B^0) = \dim(A^0 \cap B^0) \land (A \cap B \neq A) \land (A \cap B \neq \emptyset)$
- $(A \text{ disjoint } B) \iff (A \cap B = \emptyset)$

Not all relationships do apply to all object types. Overlap relationships, for instance, can only apply to area/area and line/line but not to other situations.

We implemented the dimension extended concept in our active system, described next.

4 System description

Our active spatial database prototype was implemented in Smalltalk and runs in UNIX workstations. Implementation details are omitted, since they are beyond the scope of this paper. The system is object-oriented. Since there is no standard definition for object-oriented models, we follow [Bee90]'s class-based framework. An object is an instance of a class and is characterized by its state (set of attribute values), and behavior (set of methods that can be applied to the object). An object $o$ can be constructed out of other objects $o_1,..., o_n$, in which case $o$ is called complex and $o_1,..., o_n$ are called the components of $o$. If an object is not complex, then it is called simple. Classes can be structured into inheritance hierarchies. Objects communicate with each other via methods.

4.1 Basic architecture

The active architecture had to satisfy two main criteria: adequate support for specification and management of georeferenced data; and proper integration of rules and spatial data. The solution was to combine a georeferenced data model to an active database architecture.

The first criterion was met by designing an architecture that would automatically embed spatial modelling concepts into the database data model. We chose the georeferenced object oriented data model of [CFS+94] as the basis for such an architecture. It allows separating logical specification of entities from their implementation. This presents the advantage that user defined concepts can be directly mapped into database classes, thus minimizing the mismatch between modelling and implementation.

In this model, geographic reality is modelled according to four levels: the real world level, which concerns geographic reality; the conceptual level, which describes entities at a high level of abstraction; the representation level, where different representations are defined for a given conceptual entity; and the implementation level, where the actual database structures and access methods are defined.

The second criterion – integration of rules and data – was based on extending the architecture of the Sentinel project [CAM93] with the spatial classes of the [CFS+94] georeferenced data model. Sentinel is an active object oriented database system which was developed to support multimedia DBMS for scientific applications. It must be stressed that we did not use the actual Sentinel implementation. Rather, we just adapted its active architecture description to build our prototype.

We chose the Sentinel architecture for two main reasons:

- it treats rules as objects, which unifies their management from a database point of view; and, more important,
- it also treats events as objects, which allows associating and storing several properties inside events (e.g., temporal properties, spatial dependencies). This helps the specification and maintenance of control over different types of spatio-temporal relationships.

The definition of events as objects also has the advantage of fostering an open system, since event objects can be combined by additional operators, thus extending the event algebra according to the users’ wishes.

Events can be primitive or composite. Primitive events are generated by method activation, by the system clock or raised by the application. Composite events are generated by combining primitive and composite events by means of predefined operators (e.g., sequencing or disjunction).

Like in Sentinel, our objects are classified into three main groups:

- passive: those that can accept method execution but do not generate (raise) any event;
- reactive: those where events may be generated when methods are executed;
- notifiable: those that can be notified when events are generated by reactive objects.

Reactive classes are defined as standard object classes with an additional event specification interface. This allows connecting these classes to different types of events and rules. Rules are notifiable objects. Thus, when an event is
Transformer notiﬁed and can be executed.

The notiﬁcation mechanism is based on the idea of subscription. This allows connecting rules (notiﬁable objects) to the corresponding events (rules subscribe to events raised by reactive objects). Rules can dynamically subscribe and unsubscribe to events deﬁned at reactive classes. This helps modelling the dynamics of the real world. Subscription is a means of optimizing rule activation upon event raising.

Rules can be deﬁned over an object or all objects of a class. Whereas the original Sentinel architecture speciﬁes that rules must be associated only to primitive events, we introduce the notion of subscription to composite events, speeding up rule execution.

![Figure 1: Association between rules and event objects](image)

Figure 1 shows an example of the connection among different types of objects. Reactive Object2 notiﬁes Rule2 when Event2 is raised, and Rule1 when Event3 is raised. Reactive Object1 notiﬁes Rule2 when Event1 is raised. This notiﬁcation corresponds to executing (ﬁring) the corresponding rules; it is described as “Rule2 subscribes to <Event1 raised at Object1>”, and “Rule2 subscribes to <Event2 raised at Object2>”. Passive objects cannot notify any rule, though an object can change from active to passive during its lifetime, if the user so desires. RuleN does not subscribe to any event, though again this situation may change dynamically, according to user needs.

If Reactive Object2 were a Transformer, subject to integrity constraint “Every Transformer must be placed on a Pole”, then Event2 might be an update of the Transformer’s location, and Rule2 a rule to check this constraint. An execution of the position_Transformer method (Event2) would notify this rule, whose Condition ﬁeld would contain “∃p ∈ Pole s.t. Transformer in p”.

4.2 Modelling and implementing geo-objects

The model of [CFS+94] was implemented in our prototype, with a single representation per modelled phenomenon. The world is assumed to be modelled in database classes – geo-referencing classes – whose objects describe regions of the Earth’s surface, called geo-regions. At the conceptual level, the model supports both the ﬁeld view and the object view of the world ([Con92]), distinguishing between two basic classes of database entities: geographic ﬁelds – for manipulation of continuous variables – and geographic objects – for speciﬁcation of identiﬁable entities.

As [CSE94], we also assume, for the purpose of topological constraints, the object view of the world, where a topological or vector data model represents spatial objects, and we ignore the speciﬁcation of geo-ﬁelds.

Geographic objects (geo-objects) are identiﬁable entities in the real world and can be elementary, compound or weak. They have three main components: non-spatial attributes, other geo-objects, and a Location attribute, describing the object’s spatial characteristics. The geometry of geo-objects, described at the Representation Level of the model, is described in terms of point, line and polygon features. These features are also objects belonging to the Geometric Representation class hierarchy. The location L of a geo-object is also speciﬁed as a complex object.

An elementary geo-object has no geo-objects as components. A compound geo-object is a geo-object constructed out of other geo-objects. A weak geo-object is a geo-object that contains only the location attribute and exists only as long as it is part of a (unique) compound geo-object.

In our prototype, the crucial part for expressing topological relations is the Location component of geo-objects. This was implemented as a class hierarchy, rooted at class Location, where objects are described as Points, Lines or Polygons. This hierarchy can be further specialized, according to the user’s needs. Geo-objects can be either passive or reactive, depending on the type of checking the user wants to perform on them.

A compound geo-object O can thus be described as:

\[ O \equiv \text{tuple}(\text{NonSpatial} \ldots), \text{set}(\text{Geo-objects}), L \]

Assume we want to describe a telephone network. We may then deﬁne classes CableSection (where the Location component is based on Line segments), and Connections (Location based on Point elements). Individual cable section or connection objects may be weak or elementary. Using objects from these classes, we may construct the network description as nested lists of CableSection and Connection segments. This network uses data about street location for georeferencing purposes.

This type of modelling eliminates the need for associating real world objects to layers in order to insert them in the database. A layer is simply created by identifying sets of interrelated objects (e.g., network layer), and geographic constraints among layers (e.g., telephone layer and street layer) are expressed as constraints among the respective object representations.

5 Expressing and Maintaining Constraints

Several algorithms have been reported in the literature for transforming integrity constraints expressed in a logic language into rules (e.g., [Mor84, WF90]). Since we used an object oriented database model, we adopted the mechanism of [MA94]. It consists of analyzing the constraint to identify classes and objects that may have to be checked whenever an update occurs. The database schema is then analyzed to identify additional classes to be checked (due to constraint inheritance) and to eliminate superfluous entities (given method signature).

The previous section showed how we combined a georeferenced object-oriented data model and an active database
architecture in order to obtain an active object oriented spatial prototype. This section shows how this prototype is being used to enforce topological relations expressed as constraints on geo-objects.

A constraint mechanism based on active databases relies on two processes: (1) transformation of the constraint into (E, C, A) rules, which involves event determination; and (2) maintenance of the constraint thus expressed. We assume that each binary topological relation is expressed as a constraint in a logic language\(^1\), using the topological relationships of [CevO93].

(1) Transformation Step

The transformation step we used is basically the same algorithm defined in [MA94]. This algorithm is based on generating a set of (E, C, A) rules using only constraint and database schema specification.

Initially, each constraint expression is analyzed together with the database schema and a spatial relationship table to determine which updates may violate it. Then, a set of events is generated, corresponding to pairs \((u, o_1)\) or \((u, C)\), where \(u\) is an update method (New, Delete, Modify), \(o_1\) is a specific reactive geo-object and \(C\) is the name of a reactive geo-object class. In other words, relevant events are those that update reactive geo-objects (either specific ones or any one in a given class). The concerned geo-objects must be reactive in order to notify the appropriate rules.

Event determination is divided into three categories according to the type of variables involved in the logically formulated constraint. Category1 involves Named objects (e.g., Park Tower Bldg) or constraints where all objects are bound by existential quantifiers (e.g., \(\exists c \in Cables\), where Cables is a geo-object class). Category2 involves constraints where all object variables are bound by universal quantifiers (e.g., \(\forall c, c_2 \in Cables\), \((c_1 \text{ disjoint } c_2)\)). Category3 concerns all other cases, and requires additional semantics analysis. The objects and classes involved in Category1 expressions can only be violated by Modify and Delete updates; those involved in Category2 can be violated by Modify, Delete, and Insert.

(We stress that topologic relationships are checked against the location components of geo-objects involved in a constraint. Thus, the constraint that forces a Transformer to be placed on a Pole is transformed into a constraint that checks the coincidence of the Locations of the two objects.)

The table below shows how update events are linked to the variables in a constraint. Existential quantifiers indicate that modify and delete methods may violate the constraint if applied to the Location component of the bound variable; universal quantifiers require checking of insert and modify methods; and named objects need checking upon modify or delete operations. Furthermore, additional checking may be required when deleting the last object of a class which is subject to an integrity constraint. For instance, Category2 constraint \((\forall c, c_2 \in Cables\), \((c_1 \text{ disjoint } c_2)\)) needs to be checked if a new cable \(c\) is inserted in class Cables or if the Location of an existing cable \(c\) is modified.

<table>
<thead>
<tr>
<th>Event</th>
<th>Variable</th>
<th>Named Object</th>
</tr>
</thead>
<tbody>
<tr>
<td>delete</td>
<td>modify</td>
<td>delete last</td>
</tr>
<tr>
<td>insert</td>
<td>modify</td>
<td>delete last</td>
</tr>
<tr>
<td>delete</td>
<td>modify</td>
<td>delete last</td>
</tr>
</tbody>
</table>

The generation of the (E, C, A) rules, once events are determined, is described in [MA94] and beyond the scope of this paper.

(2) Constraint Maintenance

The Constraint Maintenance process requires three steps: (a) Event detection; (b) Condition evaluation; and (c) Action execution. The event detection step is automatic in our architecture, because of the subscription mechanism. Indeed, once the events are defined at the transformation step, it is enough to make the appropriate rules subscribe to these events. Then, as soon as an update method that may violate a constraint is executed on a reactive geo-object, this object notifies the corresponding rule. This, in turn, activates the execution of the condition evaluation.

Condition evaluation corresponds to querying the space of geo-objects involved in the constraint. In our implementation, we restricted ourselves to geo-objects whose geometries are Points, LineSegments and simple convex Polygons. Consider a topological constraint that involves some relation \(R\). The basic query is find all geo-objects that have the topological relation \(R\) with the reactive geo-object which notified the rule. Thus, the query is limited, on one side, to the reactive object which raised the event, but potentially, on the other side, to the whole Location space covered by the database.

This is therefore very costly for general cases (constraints involving only class names and no named objects). Constraints which relate existing individual (named) objects are easily checked since they just affect these objects and thus need not go through the whole database upon an update.

Finally, action execution corresponds to performing a method that is defined in the notified Rule object. In our implementation, this method is limited to the abort action, i.e., updates cannot be performed if they violate a constraint. More sophisticated mechanisms can be envisaged — e.g., corrective measures, but they involve more knowledge of an application semantics.

Example:

We provide a small example to give the general idea of the mechanism. Consider the constraint that specifies that all aerial telephone cable sections must be supported by a pair of poles — i.e., each cable section is bound by a pole in each extremity. In [CevO93], these extremities are obtained by applying the boundary operators \(f\) (from) and \(t\) (to) to a line. The constraint can be defined as:

\[
\forall c \in AerialCableSection, \exists p_1, p_2 \in Pole\ s.t. \\
f(c) = p_1 \land t(c) = p_2 \land p_1 \neq p_2.
\]

Event Definition. This is a Category3 constraint (and therefore requires semantics analysis to restrict the possible events). This constraint may be violated if a cable (universally bound variable) is inserted or changes position, or if a pole (existentially bound variable) is deleted or changes position. The rules R1, R2 that check this constraint are notified by the following complex events:

\[
R_1 = \text{Event1} < \text{Insert}, c > \forall < \text{Modify}, c. \text{Loc} > \\
R_2 = \text{Event2} < \text{Delete}, p > \forall < \text{Modify}, p. \text{Loc} >
\]

where \(c.\text{Loc}\) and \(p.\text{Loc}\) are the Location components of the corresponding geo-objects.

Figure 2 shows the kinds of user actions that may violate this constraint: a CableSection may have its Location modified, or one Pole may be deleted or change Location. As well, the insertion of a new CableSection needs checking the existence of the two Poles (not shown in the figure).

\(^2\) We stress that this is a simplified example, added to help understand the mechanism. The database schema is not included for lack of space. Details are provided in [Arg93].
Constraint Maintenance. When these events are raised, the rules are notified to check the conditions. For instance, if Event1 is raised, rule R1 is fired and condition “find p1, p2 s.t. f(c) = p1.loc ∧ 1(c) = p2.loc” is checked. If the answer does not return two Poles, then the update is not allowed. Rule R2 is executed in a similar way.

6 Conclusions and future work

This paper described the use of an active spatial DBMS in the management of binary topological relations, for data in vector format. This DBMS was implemented in a prototypical form at the Computer Science Department, UNICAMP, using as a basis an extension of the architecture of the active DBMS Sentinel. The implementation, in Smalltalk, allows definition of georeferenced data according to an object-oriented model [CFS+94].

The main goal of the experiment reported here was to assess the feasibility of handling topological relations in an active database framework, with actual data. We have made some tests with simulated data and will now proceed with real test cases, which are restricted to point and line segment data.

We are also analyzing the suggestion of [CSE94] to optimize the computation of topological relations. This requires optimizing the evaluation of the condition component of the rule (i.e., spatial query optimization).

Topological relations are just an (important) subset of spatial constraints. As shown by [PS94], the 4-intersection model must be extended with orientation information in order to better express spatial relationships. Thus, an extension to this work would be to consider such a framework which, in turn, requires sophisticated orientation definitions and additional complexity in the relation checking algorithms.

At the present stage of the prototype, there is no appropriate user interface. Rather, users interact with data by means of the DBMS environment, which does not allow cartographic visualization. Thus, another extension to this work would be to provide an appropriate interface.

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